

Work - Energy Quiz Monday, Jan 22nd

Gravitational energy, E_g (book E_p for potential energy)

$$E_g = mgh$$

m is the mass, in kg

g is gravitational field strength, 9.80N/kg

h is height from a reference point, in m

- usually you set the reference at lowest point.

energy is conserved, it changes from one form to another.

eg. when you roll down a hill, gravitational energy is transformed into kinetic energy and some thermal energy (friction).

eg. a pokemon ball rolls down a 5.0m high hill. If the ball is 0.500kg , what is

- the gravitational energy at the top of the hill
- if the ball is moving at 2.0 m/s at the top of the hill, what is the kinetic energy and total energy of the ball?
- if no energy is lost due to friction, what would be the speed of the ball at the bottom of the hill?
- if the speed at the bottom of the hill is 9.0 m/s ,

how much energy was lost to frictional or rotational energies?

p224-230 Q5-12, CR 1.1-1.5

(we will go over CR 2.1-2.4 from the homework p 211 later in the class)

<http://techtv.mit.edu/videos/1491-potential-energy-to-kinetic-energy>

<https://www.youtube.com/watch?v=BVxEEn3w688&feature=fvw>

a) $E_g = mgh = 0.5 \times 9.8 \times 5 = 24.5 \text{ J}$
 ~~$\text{kg} \times \text{N} / \text{kg} \times \text{m} = \text{Nm} = \text{J}$~~

b) $E_k = \frac{1}{2} mv^2 = 0.5 \times 0.5 \times 2 \times 2 = 1.0 \text{ J}$

$E_{\text{total}} = E_g + E_k = 24.5 + 1 = 25.5 \text{ J}$

c) big idea: energy is conserved, so
total energy initial = total energy final

$$25.5 \text{ J} = E_k = \frac{1}{2} mv^2$$

$$v = \text{Sqrt}(2 \times 25.5 / 0.5) = 10.09950493836208$$

$$v = 10 \text{ m/s}$$

d) total energy initial = total energy final

$E_{gi} + E_{ki} = E_{kf} + E_{\text{lost}}$ (E_g is zero at the bottom, that is where you set $h=0$)

$$25.5 \text{ J} = 0.5 \times 0.5 \times (9^2) + E_{\text{lost}}$$

$$E_{\text{lost}} = 25.5 - (0.5 \times 0.5 \times (9^2)) = 5.25 \text{ J lost to}$$

$$25.5 - 0.5 \times 0.5 \times (9^2) = E_{\text{lost}}$$

$E_{\text{lost}} = 25.5 - (0.5 \times 0.5 \times (9^2)) = 5.25 \text{ J lost to frictional or rotational effects}$

<https://www.youtube.com/watch?v=PplaBASQ3M>

Work - Energy Quiz Monday, Jan 22nd
 Double block day - rocket lab south field - bring boots/rain stuff - group of 3-5
 test - end of the next week - Feb 2nd ?

Gravitational energy and conservation of energy.

Last class - work energy theorem -

$W = \text{change in energy}$

used to derive the equation for kinetic energy

$$E_k = \frac{1}{2}mv^2$$

We do the same thing for gravitational energy

$$W_g = \Delta E_g$$

work done against gravity = the change in

gravitational energy

$$W = Fd$$

$$W_g = F_g d = mgd = \Delta E_g$$

d is the displacement up/down, = change in height

$$mg\Delta h = \Delta E_g$$

thus

$$E_g = mgh$$

E_g is the gravitational energy, in Joules, J.

m is the mass, in kg

g is gravitational field strength, 9.8N/kg near Earth.

h is the height relative to a reference point, in m
usually you choose the lowest point as the reference point.

Big Idea - Energy is conserved

Total of all the types of energy initial = total of all the types of energy final

$$E_{\text{total } i} = E_{\text{total } f}$$

eg. A 2.0 kg tire rolls down a 5.0 m high hill.

What is the

a) initial gravitational energy of the tire?

$$E_g = mgh = 2.0 \text{ kg} \times 9.8 \text{ N/kg} \times 5.0 \text{ m} = 98 \text{ J}$$

a) if the tire starts out moving at 4.0 m/s, what is the initial kinetic energy of the tire?

$$E_k = \frac{1}{2} mv^2 = 0.5 \times 2.0 \text{ kg} \times (4 \text{ m/s})^2 = 16 \text{ J}$$

a) What is the total initial energy of the tire?

$$E_{\text{total}} = E_g + E_k = 98 + 16 = 114 \text{ J}$$

a) if all the energy of the tire goes to kinetic energy as it rolls down the hill, how fast is it going at the bottom?

$$E_{\text{total}} = E_k = \frac{1}{2} mv^2$$

$$v = \text{Square root} (2 \times E_k / m)$$

$$v = \text{Sqrt}(2 \times 114 / 2) = 10.67707825203131$$

$$v = 11 \text{ m/s}$$

a) if the speed of the tire at the bottom of the hill is only 9.0 m/s, how much energy was lost to friction or rotational effects?

$$E_{\text{total i}} = E_{\text{total f}}$$

$$114 \text{ J} = E_k + E_{\text{lost}} \quad (E_g = 0 \text{ at lowest point})$$

$$114 \text{ J} = 0.5 \times 2 \times (9^2) + E_{\text{lost}}$$

$$E_{\text{lost}} = 114 - (0.5 \times 2 \times (9^2)) = 33 \text{ J}$$

p224-230 Q5-12 CR 1.1-1.5